

Webinar



Sciences Economiques et
Sociales de la Santé et Traitement
de l'Information médicale
sesstim.univ-amu.fr

&



openhealth-institute.org

Constantinos SIETTOS

School of Applied Mathematics and Physical Sciences National Technical
University of Athens, Greece

From Agent-Based Models on Complex Networks to the Risk Assessment of Emergent Infectious Disease Dynamics: from Simple Mathematical Models to Real Epidemics

avril 2017



Cliquez ici pour voir l'intégralité des ressources associées à ce document



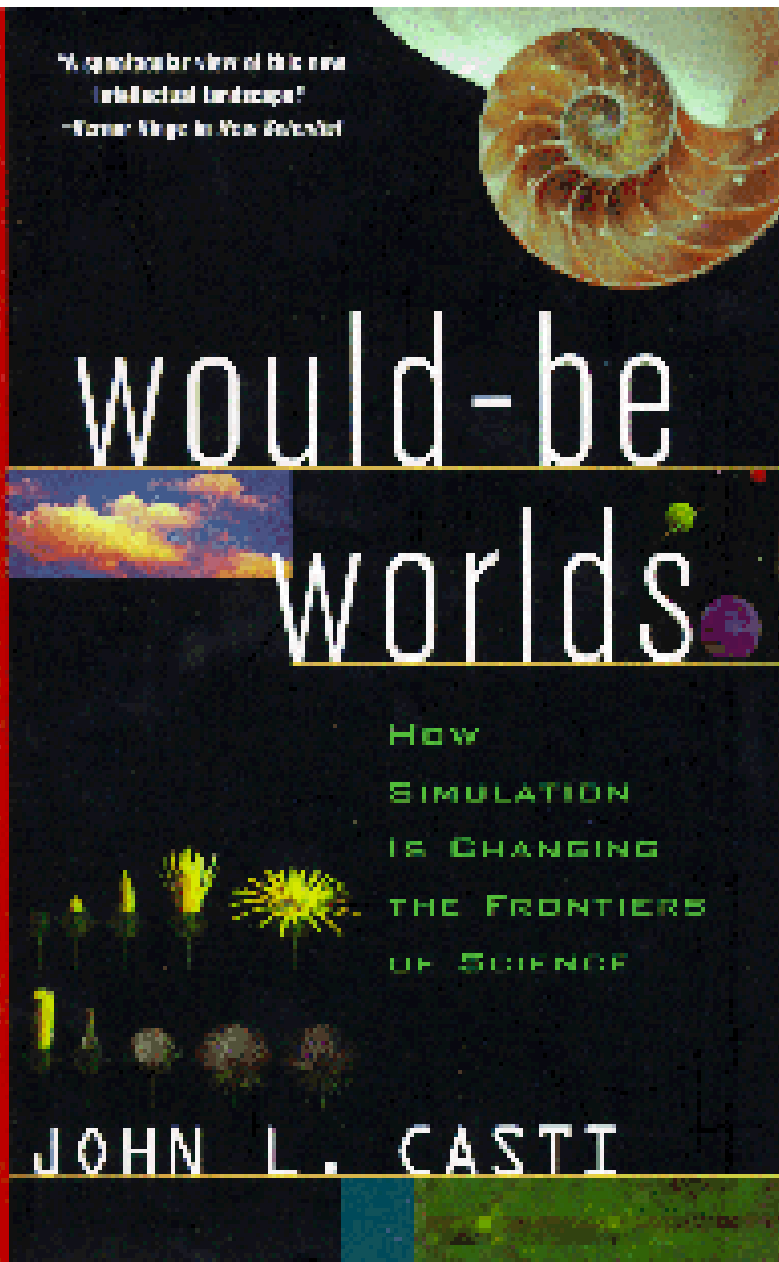
From Agent-Based Models on Complex Networks to the Risk Assessment of Emergent Infectious Disease

Dynamics: from Simple Mathematical Models to Real Epidemics

Constantinos Siettos

School of Applied Mathematics and Physical Sciences
National Technical University of Athens, Greece

SESSTIM/OHI Webinars, April 2017



....the ability to create surrogate versions of real complex systems inside our computing machines changes the way we do science. In particular, emphasis will be laid upon the idea that these so-called, “artificial worlds” play the role of laboratories for complex systems, laboratories that are completely analogous to the more familiar laboratories that have been used by physicists, biologists, and chemists for centuries to understand the workings of matter.

Because the ability to do controlled, repeatable experiments is a necessary precondition to the creation of a scientific theory of anything, the argument will be made that, for perhaps the first time in history, we are now in a position to think realistically about the creation of a theory of complex systems.



Agent-based Models and Complexity

Agent-Based models that simulate the simultaneous operations and interactions of multiple objects (atoms, molecules, agents) in an attempt to re-create and predict the appearance of complex phenomena.

The process is one of emergence from the lower (micro) level of systems to a higher (macro) level.

As such, a key notion is that simple behavioral rules generate complex behavior.

Complex vs. Complicated

Collective patterns emerging from many interacting components, The emergent dynamics is more than the sum of the properties of the individual units

...decomposing the system and analyzing subunits does not necessarily give us an idea of the behavior as a whole

...the behavior of complex systems is therefore unpredictable



...subunits are designed and connected so that they accomplish a pre-determined (predictable) function

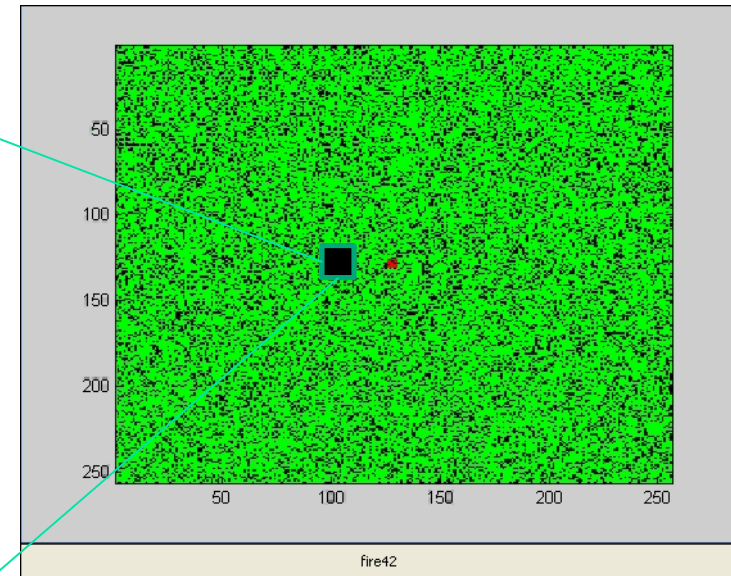
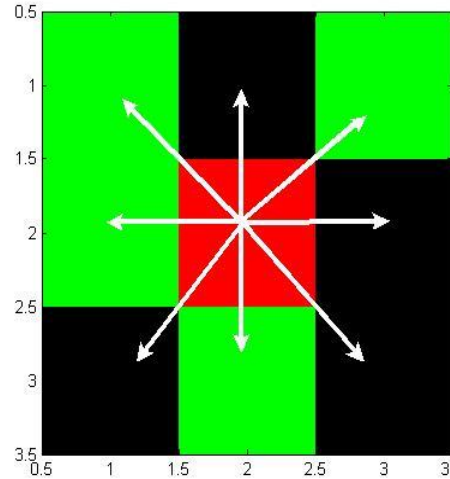
The notion of Complexity: a simplistic! model of Tumor Growth

A cell can take each time one of the three states:

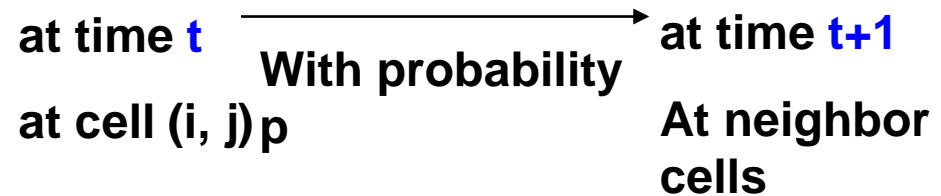
- 1: Black, tumor cell
- 2: Green, healthy cell.
- 3: Red: micro vessel cell

The evolution rules are the following:

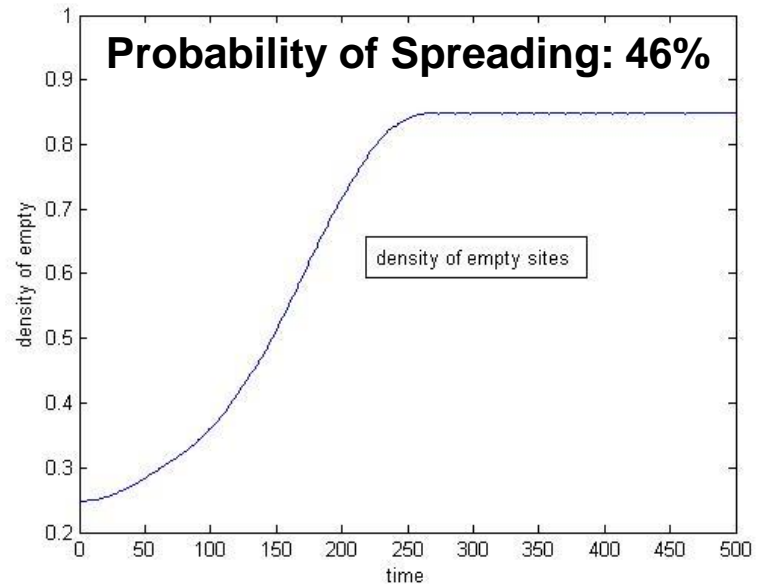
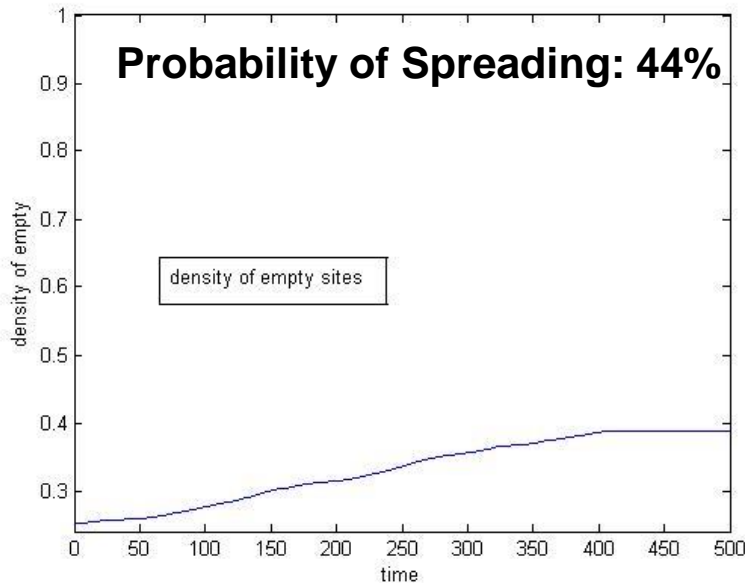
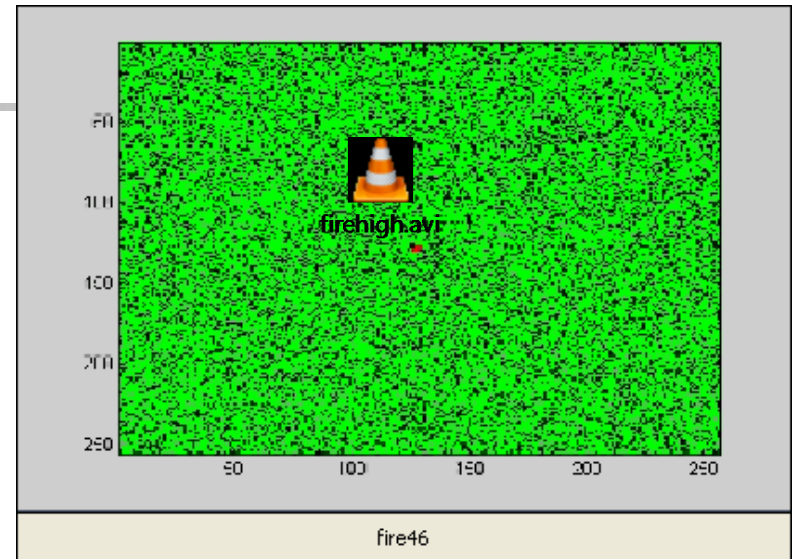
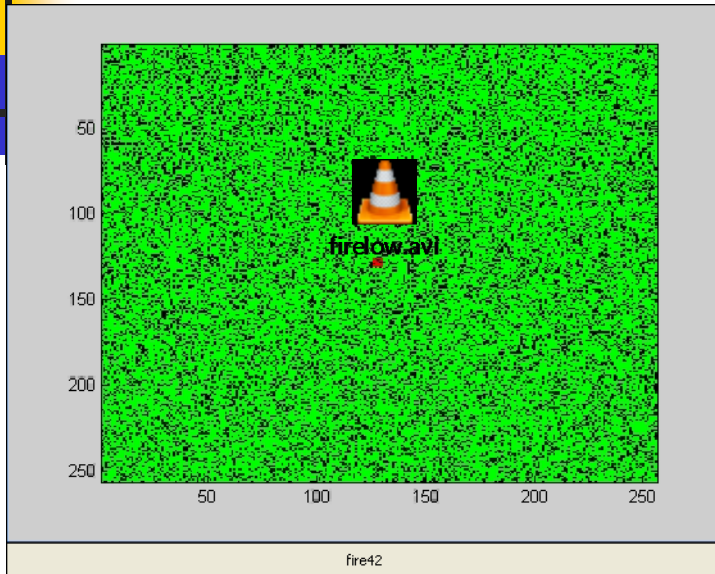
- Micro vessel on a site will invade to nearest neighbors healthy cells at the next time step with probability p .
- All cells with micro vessel will turn to tumor at the next time step.

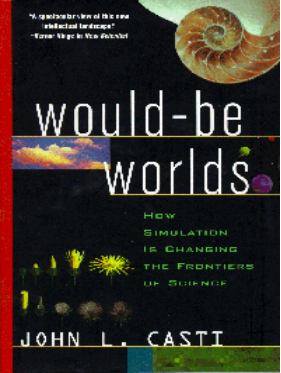


Cells with Micro vessel



The notion of Complexity: simple behavioral rules generate complex behavior. Tumor growth



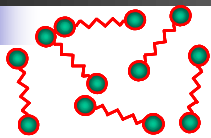


20 years after....

A Big! number of available microscopic/ agent-based models simulating the time evolution of Complex Systems (Biological Systems, Material Science, Complex Fluids, Epidemics, Neurons)

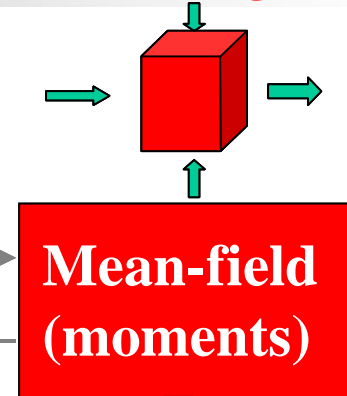
Micro-Scale

Macro Emergent) Scale



Large-Scale Microscopic Models

Agent-Based
Brownian D
Monte Carlo
Molecular Dynamics



Mean-field (moments)

ODE's-PDE's

**Different time and space scales
Macro scales much much bigger
than the bigger Microscopic
scale**

**The analysis is usually sought
at this level (system-level analysis)**

**... but such good models not always exist
in closed form**

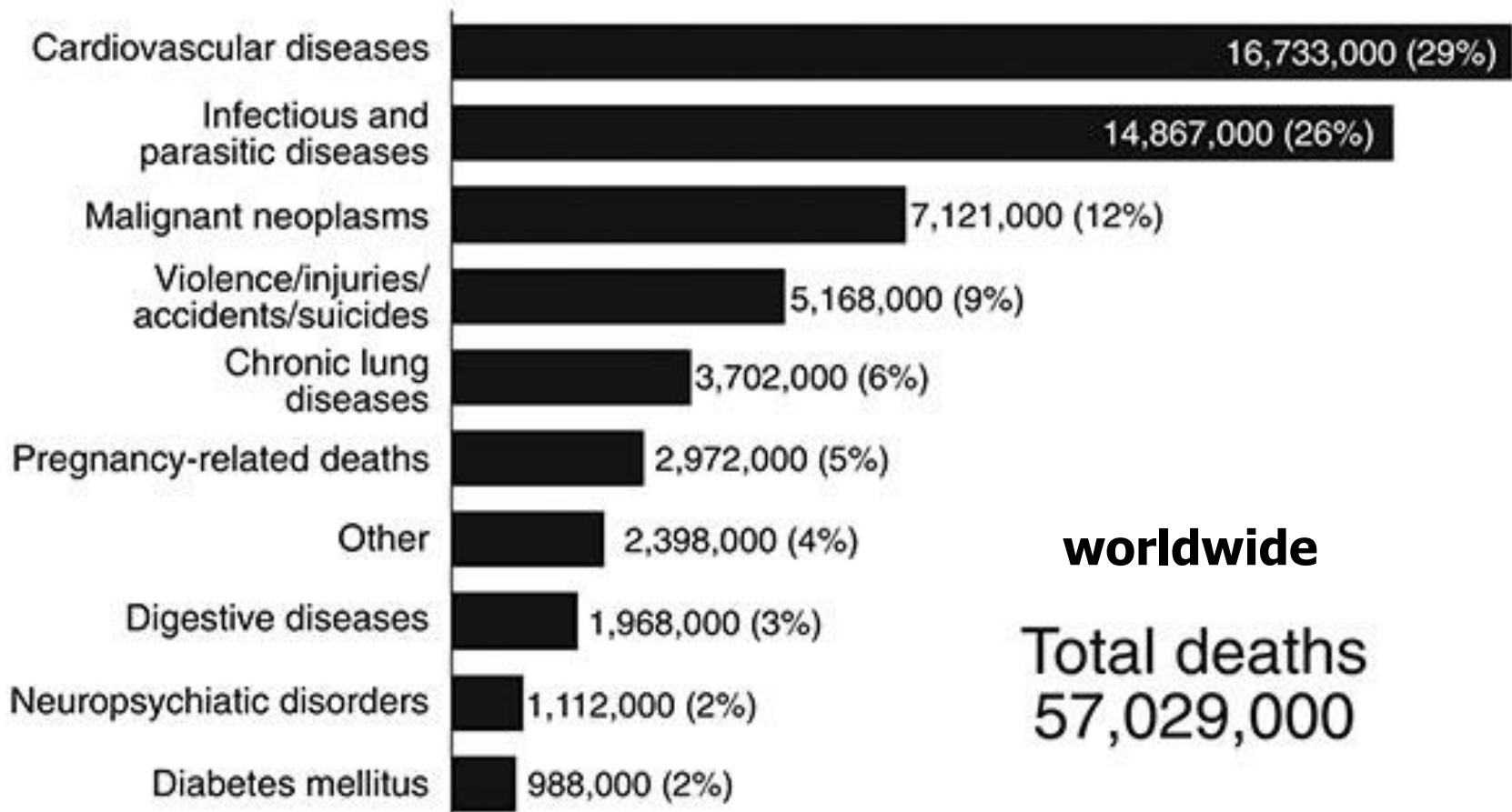
- Material Science
- Epidemiology
- Bio
- Neurons
- Markets

Epidemics: One of the major challenges nowadays

The surveillance, analysis and ultimately the efficient long-term prediction and control of epidemic dynamics appear to be (the) major challenges nowadays



Centers for Disease Control and Prevention
CDC 24/7: Saving Lives, Protecting People™



worldwide
Total deaths
57,029,000

Epidemics: One of the major challenges nowadays

The surveillance, analysis and ultimately the efficient long-term prediction and control of epidemic dynamics appear to be (the) major challenges nowadays

Influenza Pandemics 20th Century



Credit: US National Museum of Health and Medicine

1918: “Spanish Flu”
A(H1N1)

20-40 m deaths

675,000 US deaths



1957: “Asian Flu”
A(H2N2)

1-4 m deaths

70,000 US deaths



1968: “Hong Kong Flu”
A(H3N2)

1-4 m deaths

34,000 US deaths

Epidemics: One of the major challenges nowadays

Ebola outbreaks

To January 14th 2016

Number of people:

● infected

of whom:

● dead

3,804

2,536

14,122

3,955

10,675

4,809

86

208

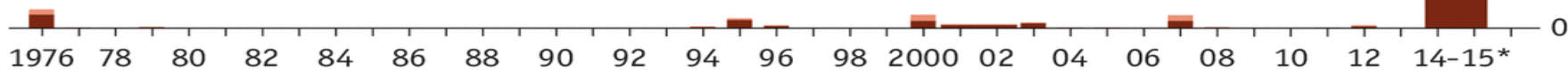
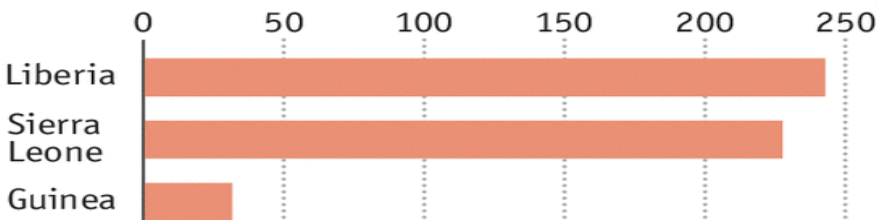
6649

28,637

11,315

Number of people infected

Per 100,000 population



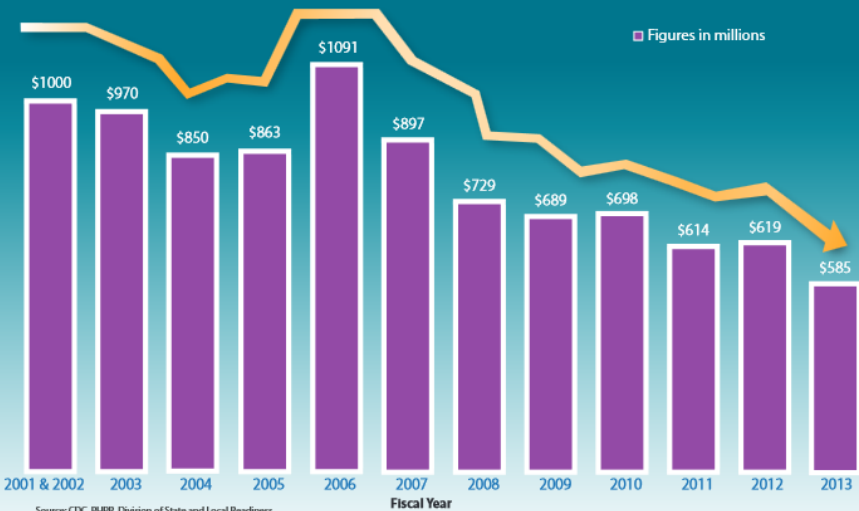
Sources: WHO; UN; *The Economist*

*Includes cases in Italy, Spain, Britain and the United States. Excludes Congo

Epidemics arise: funding... declines...

CDC continues to work with reduced financial resources, which similarly affects state, local, and insular area public health departments

Public Health Emergency Preparedness (PHEP) Cooperative Agreement Funding¹



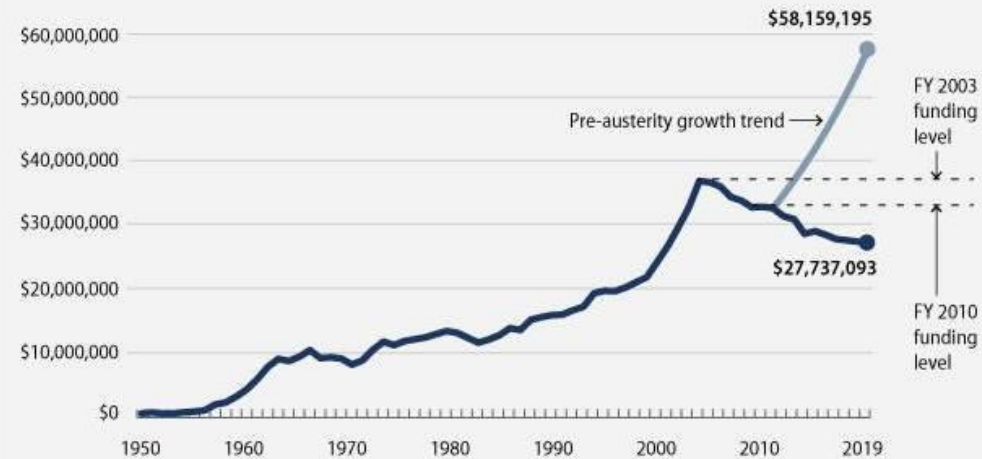
Source: CDC, PHPR, Division of State and Local Readiness

¹Totals include the following: PHEP Base Funding, Cities Readiness Initiative, Chemical Laboratory Capacity, Early Warning Infectious Disease Surveillance (EWDS), Real-Time Disease Detection, Risk Funding, Smallpox, Pan Flu Supplement - Phase I, Pan Flu Supplement - Phase II, and Pan Flu Supplement - Phase III Funding. The FY2008 totals include \$24 million for pandemic influenza preparedness projects that were from a different funding opportunity announcement.

FIGURE 2

NIH funding, FY 1950–2019

in thousands of constant 2013 BRDPI adjusted dollars



Source: NIH funding figures through FY 2014 are based on total budget authority. Projected NIH funding figures for FY 2015 through FY 2019 are based on data from the Congressional Budget Office.

Modelling Epidemics : the difficulties

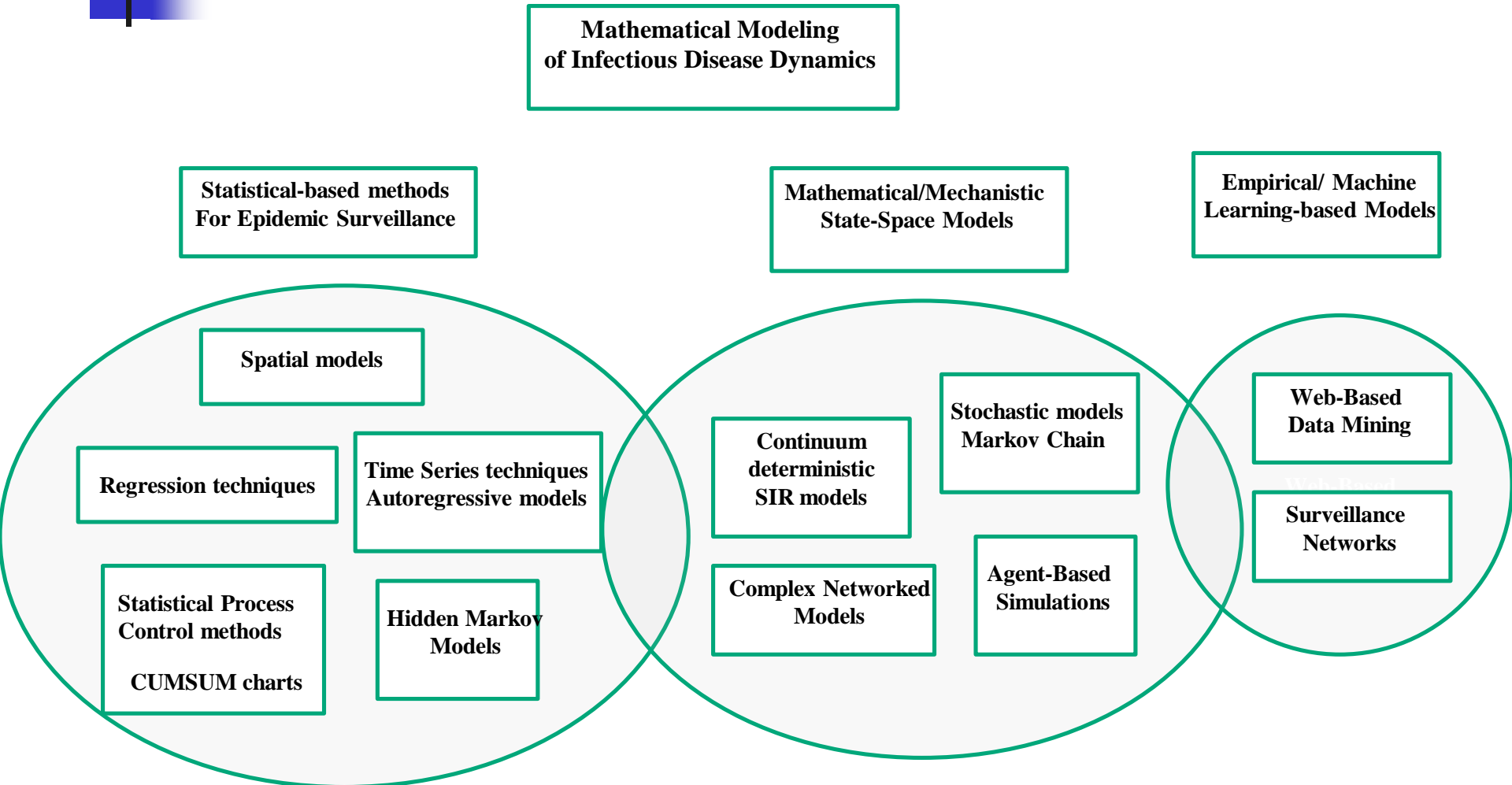


Modelling difficulties stem mainly from three reasons:

- (a) the continuous and ever-lasting mutations of pathogens, particularly of viruses**
- (b) the complexity in the disease host-pathogen and host-host transmission mechanisms,**
- (c) the complexity in the structure of underlying social network,**

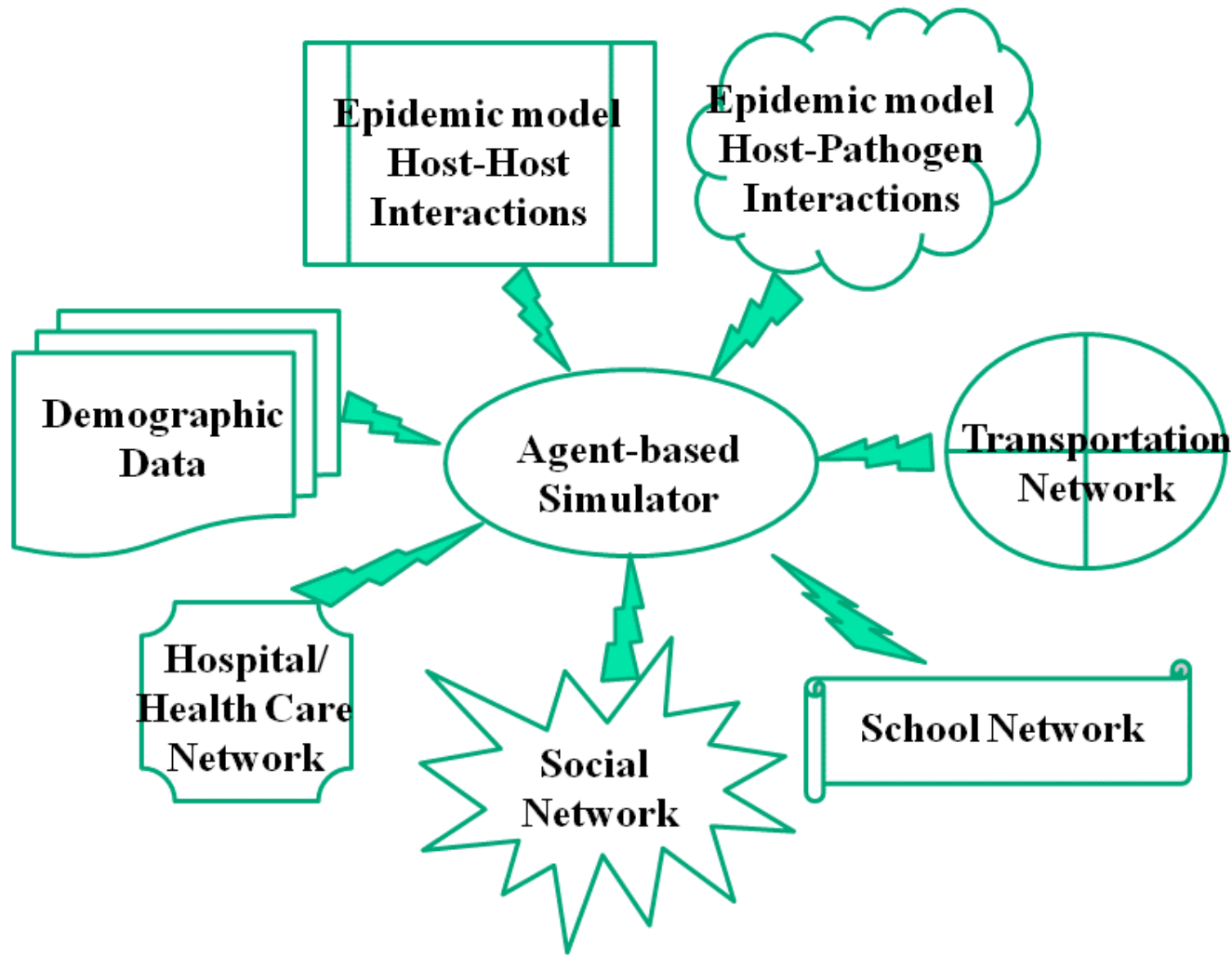
Epidemic modelling: an overview

Siettos, C. I., Russo, L., 2013, Mathematical Modeling of Infectious Disease Dynamics: A Review, Virulence, 4 (4), 295-306.



An Agent-Based Simulator

the Models of Infectious Disease Agent Study (**MIDAS**), a network launched on May, 1, 2004 and funded by the U.S. National Institutes of Health has as its pilot effort the detailed modeling of the dynamics of a hypothetical flu pandemic



What is done until now with Agent-Based Simulators



(A) Run in time:

running many scenarios with different initial conditions and for long times to get the relative macroscopic information.



(B) Try to find Macroscopic equations in a closed form
→ Statistical Mechanics

What is done until now: an example for obtaining closures with the pencil

Example: The SIRS model for Epidemics.

Use of stochastic dynamics on a lattice

(or more general graphs)

Description

A site \mathbf{x} of a d -dimensional graph can be:

S (healthy and susceptible)

I (infected)

R (recovered, i.e., healthy and immune).

The rules:

$S \longrightarrow I$ with rate $\lambda \eta(\mathbf{x})$,
 $\eta(\mathbf{x})$ number of Infected Neighbors

$I \longrightarrow R$ with rate δ

$R \longrightarrow S$ with rate γ

What is done until now: an example for obtaining closures with the pencil

Mathematical individual description of SIRS

$$\frac{dP_t(S_x)}{dt} = -\lambda \sum_{y \in N(x)} P_t(S_x, I_y) + \gamma P_t(R_x)$$

$$\frac{dP_t(I_x)}{dt} = +\lambda \sum_{y \in N(x)} P_t(S_x, I_y) - \delta P_t(I_x)$$

$$\frac{dP_t(R_x)}{dt} = \delta P_t(I_x) - \gamma P_t(R_x) \quad (\delta = 1)$$

$N(x)$: Is the neighborhood (nearest-neighbor sites) of a site **x**

$P_t(a_x)$: is the probability of having a state **a** at site **x** at, **$a = S, I, R$**

$P_t(a_x, b_y)$: is the joint probability to have state **a** at site **x** and state **b** at site **y** .

Problem : Equations are, as is usual for moment equations, not in a closed system.

What is done until now: an example for obtaining closures with the pencil

Problem : This leads to an infinite hierarchy.

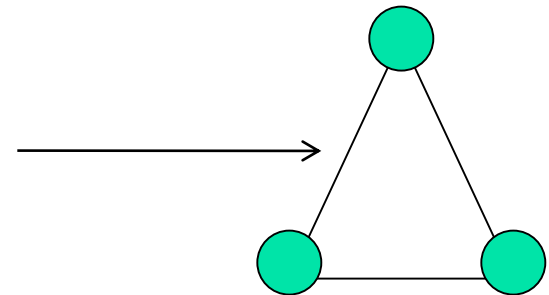
To solve such a hierarchy, one usually resorts to some **approximation-reduction scheme, which expresses the higher-order moments in terms of the lower-order ones and truncates the equations at some point.**

To close the system and derive a set of autonomous equations we approximate the triad joint probability

$$P(a_x, b_y, x_w) = \frac{P(a_x, b_y)P(b_y, x_w)}{P(b_y)}$$

Assumption

Three adjacent sites can not form a triangular



Objective

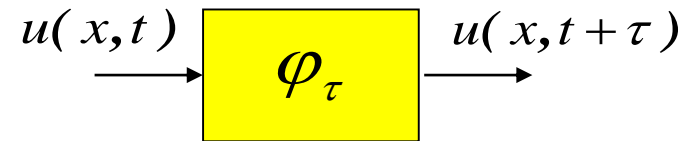
Bridge the gap between micro (where the information is available) and macro scales (where the analysis is sought)

Enable microscopic simulators through a computational superstructure to perform tasks beyond simple simulation

- **Obtain coarse stable and unstable!!! steady state solutions from microscopic simulator**
- **Accelerate convergence of microscopic simulator to the corresponding coarse steady state**
- **Calculate “coarse” slow eigenvalues and eigenvectors**
- **Design linear and nonlinear controllers : Nonlinear feedback linearization**
- **Deal with Rare Events**

without having the equations!

I don't know the coarse equations, but I have a black box agent-based simulator



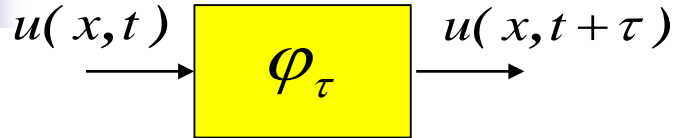
Use the agent-based simulator as an experiment!

Identify coarse information on demand

THE CONCEPT: What else can I do with an integration code ?

Have Equations (PDE's)

Write Simulation



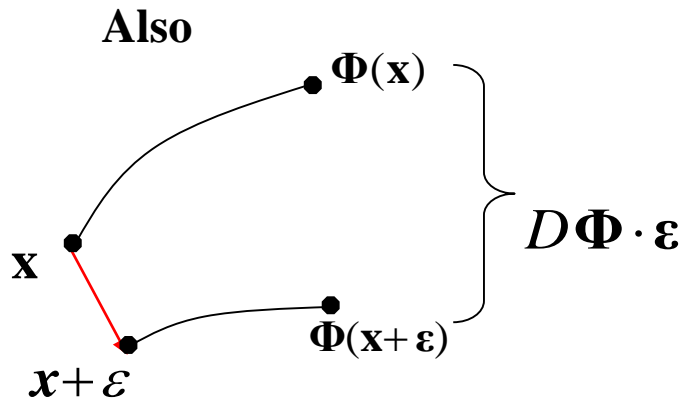
Large-Scale Systems

Jacobian too big to apply direct solvers
(e.g. Newton-Raphson, Jacobi)



-Instead, use iterative linear algebra methods

(matrix-free methods)



Estimate
matrix-vector
product
↓
Matrix free
iterative linear
algebra
↓
The World



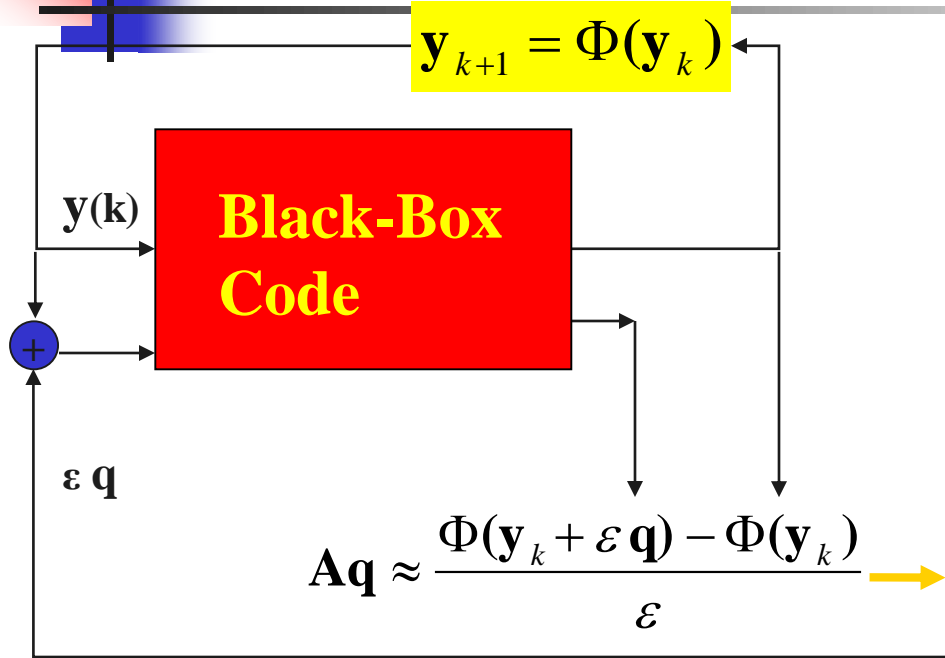
CG, GMRES
Arnoldi
Newton-Krylov

Matrix-free methods: Arnoldi Eigensolver & GMRES

No need of “transparent” equations, just a black box code that will integrate it over a step size that it has been chosen.

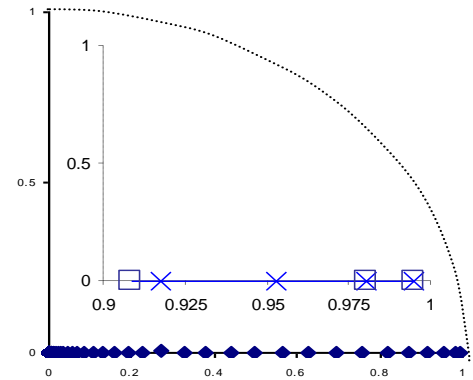
SYSTEM AROUND THE STEADY STATE

GMRES → SOLVE AX=B



Critical Eigenvalues

ARNOLDI



Set q_1 with $\|q_1\| = 1$

For $j=1,m$

(1) Calculation Aq_j

(2) Calculation $h_{t,j} = \langle Aq_j, q_t \rangle, t = 1, 2, \dots, j$

(3) $r_j = Aq_j - \sum_{t=1}^j h_{t,j} q_t$

(4) $h_{j+1,j} = \langle r_j, r_j \rangle^{1/2}$

(5) $q_{j+1} = r_j / h_{j+1,j}$

End For

In step m the algorithm creates an orthogonal basis in Krylov subspace K_m

$$Q_m = \{q_1, Aq_1, \dots, A^{m-1}q_{m-1}\}$$

The projection of A in K_m results to an upper Hessenberg $H_m = Q_m^T A Q_m$ with elements h_{ij}

Computational Methods for System-Level Analysis

What if physics are known in a more detailed (microscopic) level?



...but there is no description (in moments of distribution) of the macroscopic behavior;

**SIMPLE SIMULATION:
LIKE EXPERIMENTAL
EXPERIMENTS**

i.e. run atomistic-based models for many agents and for different parameters and for long time to get macroscopic (system-level) information

MICRO-scopic

MACRO-scopic

FINITE ELEMENTS

**KRYLOV SUBSPACE
ARNOLDI-GMRES**

**NEWTON/
(QUASI-NEWTON)**

CONTROL

OPTIMIZATION

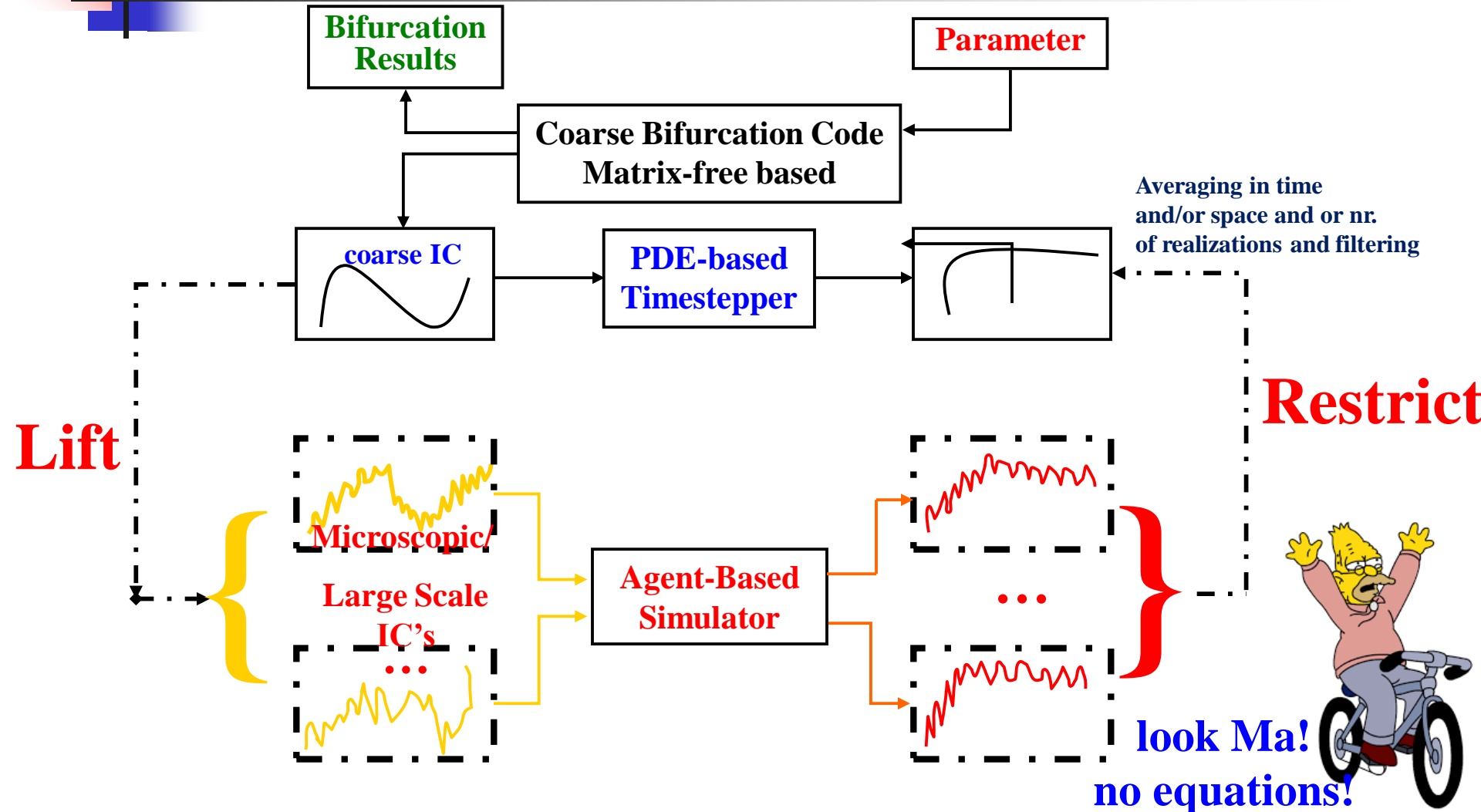
AIM: Systematically bridge the gap between Micro-scopic and Macro-scopic (system-level) World

But good macroscopic models do not always exist in closed form ...

An Equation-Free Approach

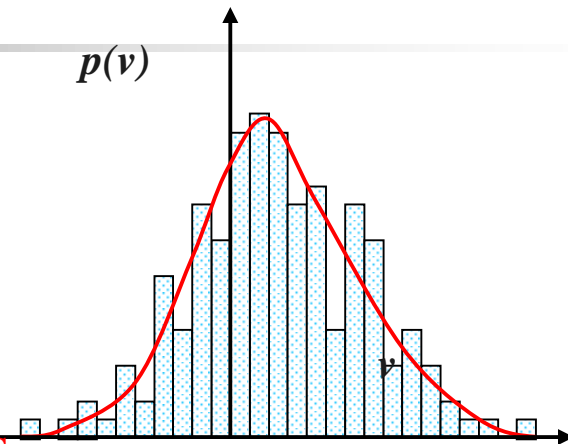
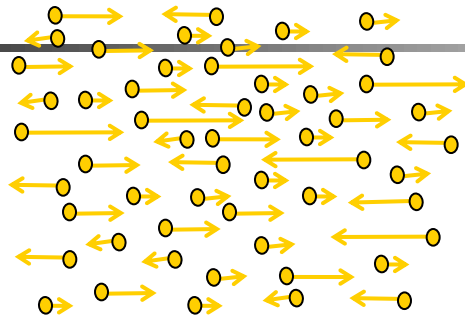
.... or else How to find solutions without the equations

[Kevrekidis et al., *Comm. Math. Sciences*, 1, 715-762, 2003;
Siettos, Gear and Kevrekidis, *EPL*, *EPL*, 99, 48007, 2012]



The Assumption: Time Scale Separation of Distributions and Moments

Macroscopic models exist (but the problem is too complex & we can't derive them) and close for the expected behaviour of a few low moments of the evolving distributions



Descriptions

1. Detailed: v_i for each variables
2. Moments

$$m_0 \quad \text{Zeroth moment: density } \rho \quad \int p(v)dv$$

$$m_1 \quad \text{First moment: momentum } \rho v \quad \int p(v)v dv$$

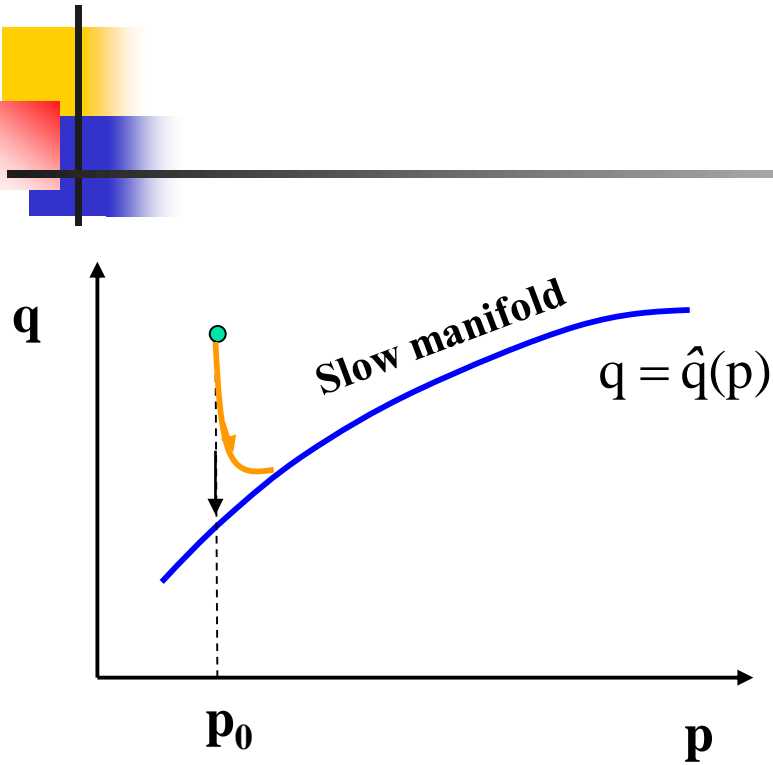
m_2 Second moment

m Third Moment

3

↓ Time scale separation

SLOW & FAST DYNAMICS



$$\frac{dp}{dt} = f(p, q)$$

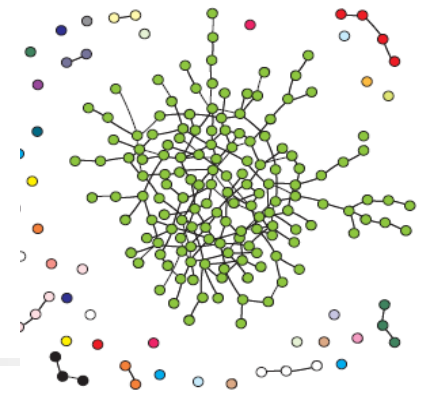
$$\frac{dq}{dt} = \frac{1}{\varepsilon} g(p, q)$$

$$\varepsilon \text{ small} \rightarrow \left. \begin{array}{l} g(p, q) \approx 0 \\ q \approx \hat{q}(p) \end{array} \right\} \begin{array}{l} \text{very} \\ \text{fast} \end{array}$$

So soon $\dot{p} = f(p, q) \approx f(p, \hat{q}(p)) \equiv \tilde{f}(p)$

Singular perturbed systems

Motivation/Scope



- ✓ Introduce methods for analysing the EMERGENT DYNAMICS of detailed Agent-based evolving on complex networks (BIFURCATION ANALYSIS, STABILITY...)
- ✓ Introduce methods for tuning topological characteristics of contact transmission networks to get closer to the structure of real-world observations.
- ✓ Explore the effects of the network topology on the Emergent Dynamics of Agent-Based Epidemic Models.
- ✓ Examine how graph-base intervention policies can be introduced along with the use of the network topological characteristics (CONTROL DESIGN)

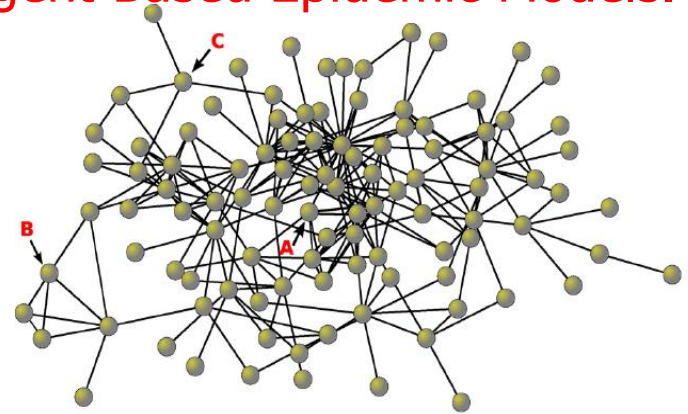
USING THE AGENT-BASED SIMULATOR AS EXPERIMENT, THUS BYPASSING THE NEED FOR DERIVING ANY MACROSCOPIC MODEL IN A CLOSED FORM

The Problems

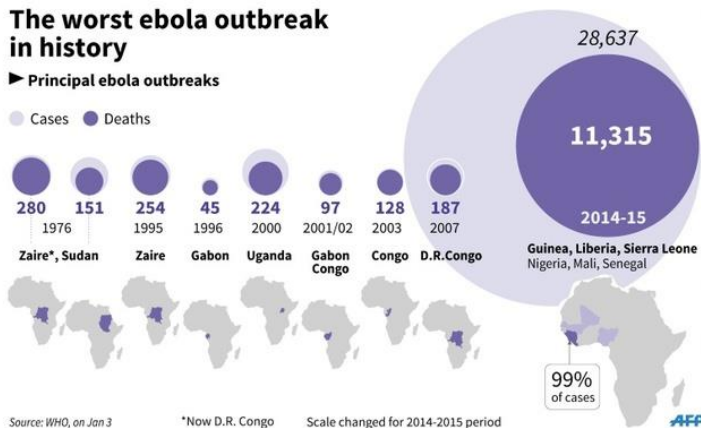
1. Comparison between closed Models and Equation-Free Computations



2. Exploring the effects of the Network Topology on the Emergent Dynamics of Agent-Based Epidemic Models.



3. Forecasting 2014 Ebola Epidemics



1. The Epidemic model: The Efficiency of Closures

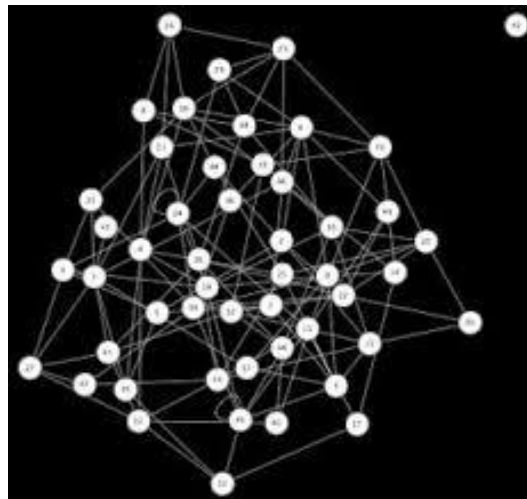
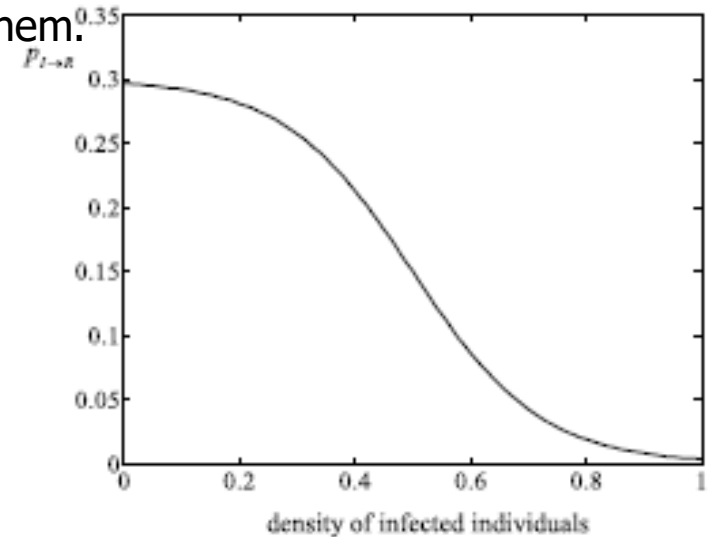
Reppas, A., De Decker Y., Siettos, C.I., 2012, On the Efficiency of the Equation-Free Closure of Statistical Moments: Dynamical properties of a Stochastic Epidemic Model on Erdos-Renyi networks, *Journal of Statistical Mechanics: Theory and Experiment*, 8, P08020.

Rule #1: An infected individual [I] infects a susceptible (S) neighbor with a probability

$$p_{S \rightarrow I} = \lambda \quad \text{if an active link exists between them.}$$

Rule #2: An infected (I) individual recovers with a probability $p_{I \rightarrow R} = \delta$

Rule #3: A recovered individual becomes susceptible with a probability $p_{R \rightarrow S} = \gamma$



Contact transmission
Network:
Erdős-Rényi

1. The Epidemic model: the Efficiency of Closures

Reppas, A., De Decker Y., Siettos, C.I., 2012, On the Efficiency of the Equation-Free Closure of Statistical Moments: Dynamical properties of a Stochastic Epidemic Model on Erdos-Renyi networks, *Journal of Statistical Mechanics: Theory and Experiment*, 8, P08020.

Mean Field

$$P_t(a_x, b_y) = P_t(a_x)P_t(b_y)$$

$$P_t(a_x, b_y, c_w) = P_t(a_x)P_t(b_y)P_t(c_w).$$

$$\begin{aligned}\frac{d[S]}{dt} &= -\lambda z[S][I] - \gamma(1 - [S] - [I]) \\ \frac{d[I]}{dt} &= \lambda z[S][I] - \delta[I]\end{aligned}$$

Kirkwood (pairwise)

$$P_t(a_x, b_y, c_w) = \frac{P_t(a_x, b_y)P_t(b_y, c_w)}{P_t(b_y)}.$$

$$\begin{aligned}\frac{d[I]}{dt} &= \lambda z[SI] - \delta[I] \\ \frac{d[R]}{dt} &= \delta[I] - \gamma[R] \\ \frac{d[SR]}{dt} &= \delta[SI] + \gamma([R] - [RI] - 2[SR]) - \frac{(z-1)\lambda[SI][SR]}{1 - [R] - [I]} \\ \frac{d[RI]}{dt} &= -(2\delta + \gamma)[RI] + \delta([I] - [SI]) + \frac{(z-1)\lambda[SI][SR]}{1 - [R] - [I]} \\ \frac{d[SI]}{dt} &= \gamma[RI] - (\lambda + \delta)[SI] + \frac{(z-1)\lambda[SI]}{1 - [R] - [I]}(1 - [R] - [I] - [SR] - 2[SI])\end{aligned}$$

1. The Epidemic model: the Efficiency of Closures

Reppas, A., De Decker Y., Siettos, C.I., 2012, On the Efficiency of the Equation-Free Closure of Statistical Moments: Dynamical properties of a Stochastic Epidemic Model on Erdos-Renyi networks, *Journal of Statistical Mechanics: Theory and Experiment*, 8, P08020.

Ursell Expansion (pairwise)

$$P_t(S_x, S_y, I_w) = P_t(S_x)P_t(S_y, I_w) + P_t(I_w)P_t(S_x, S_y) - P_t(S_x)P_t(S_y)P_t(I_w)$$

$$P_t(I_w, S_x, I_y) = 2P_t(I_w)P_t(S_x, I_y) - P_t(I_w)P_t(S_x)P_t(I_y)$$

$$P_t(I_w, S_x, R_y) = P_t(R_x, S_y, I_w) = P_t(I_w)P_t(S_x, R_y) + P_t(R_y)P_t(I_w, S_x)$$

— ↓

$$\frac{d[I]}{dt} = \lambda z[SI] - \delta[I]$$

$$\frac{d[R]}{dt} = \delta[I] - \gamma[R]$$

$$\begin{aligned} \frac{d[SR]}{dt} &= \delta[SI] + \gamma([R] - [RI] - 2[SR]) - (z - 1) \\ &\quad \times \lambda([I][SR] + [R][SI] - [I][R](1 - [I] - [R])) \end{aligned}$$

$$\begin{aligned} \frac{d[RI]}{dt} &= -(2\delta + \gamma)[RI] + \delta([I] - [SI]) \\ &\quad + (z - 1)\lambda([I][SR] + [R][SI] - [I][R](1 - [I] - [R])) \end{aligned}$$

$$\begin{aligned} \frac{d[SI]}{dt} &= \gamma[RI] - (\lambda + \delta)[SI] + (z - 1)\lambda([SI](1 - [I] - [R]) + [I] \\ &\quad \times (1 - [I] - [R] - [SR] - [SI]) - [I](1 - [I] - [R])^2) \\ &\quad - (z - 1)\lambda(2[I][SI] - [I]^2(1 - [I] - [R])). \end{aligned}$$

1. The Epidemic model: the Efficiency of Closures

Reppas, A., De Decker Y., Siettos, C.I., 2012, On the Efficiency of the Equation-Free Closure of Statistical Moments: Dynamical properties of a Stochastic Epidemic Model on Erdos-Renyi networks, *Journal of Statistical Mechanics: Theory and Experiment*, 8, P08020.

Bethe-type Ansatz (pairwise)

$$P_t(S_x, S_y, I_w) = P_t(S_x)P_t(S_y, I_w)$$

$$P_t(I_w, S_x, I_y) = P_t(I_y)P_t(I_w, S_x)$$

$$P_t(I_w, S_x, R_y) = P_t(R_y)P_t(I_w, S_x)$$

$$P_t(R_x, S_y, I_w) = P_t(R_x)P_t(S_y, I_w).$$

$$\frac{d[I]}{dt} = \lambda z[SI] - \delta[I]$$

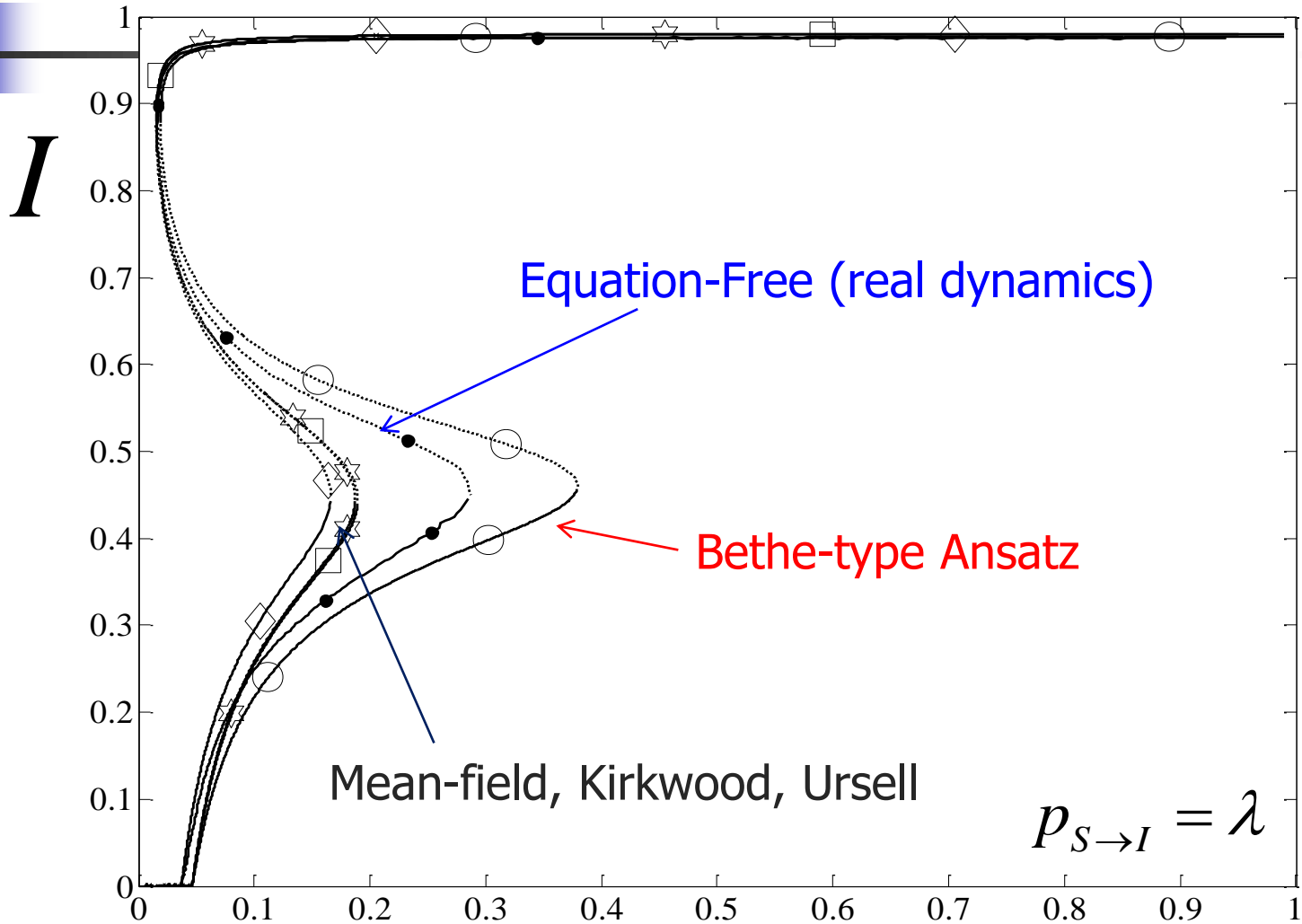
$$\frac{d[R]}{dt} = \delta[I] - \gamma[R]$$

$$\frac{d[SR]}{dt} = \delta[SI] + \gamma([R] - [RI] - 2[SR]) - (z - 1)\lambda([R][SI])$$

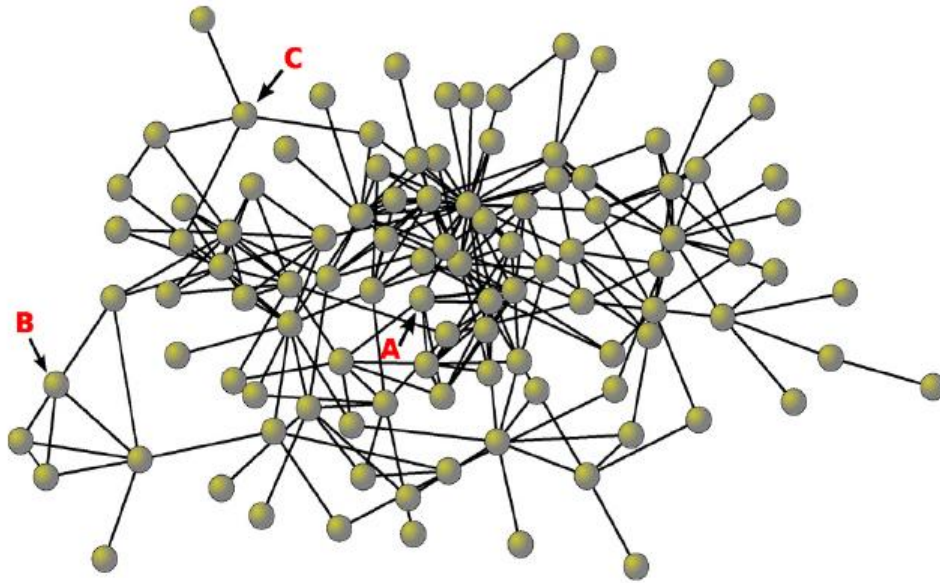
$$\frac{d[RI]}{dt} = -(2\delta + \gamma)[RI] + \delta([I] - [SI]) + (z - 1)\lambda([R][SI])$$

$$\frac{d[SI]}{dt} = \gamma[RI] - (\lambda + \delta)[SI] + (z - 1)\lambda[SI](1 - [R] - 2[I]).$$

1. Closures vs Equation-Free/Bifurcation Diagram



2. Epidemics: The importance of Network Topology: the clustering coefficient and path length: strong and weak links



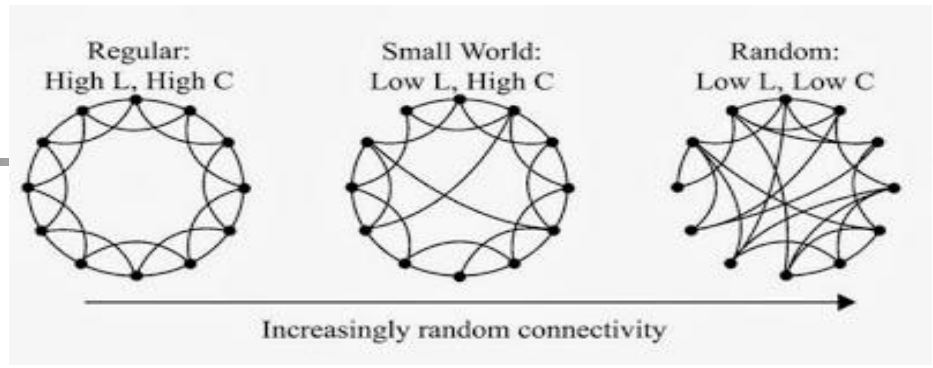
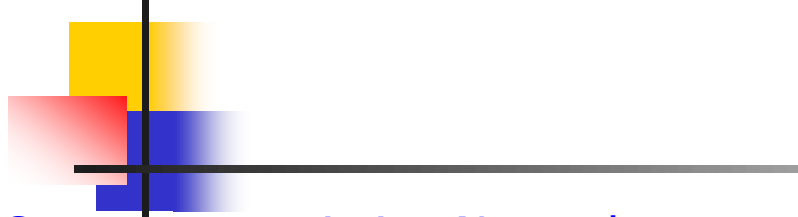
Christakis N., Fowler J., Social Network Sensors for Early Detection of Contagious Outbreaks, PLoS ONE 5(9) 2010.

A real network of students in the University of Harvard which is used to examine the progress of a disease (Christakis & Fowler, 2010).

Node **A** is a **central node** with 6 friends around him was more likely to get infected sooner **because of its shortest path length** from other individuals in the network (e.g. **B** & **C**)

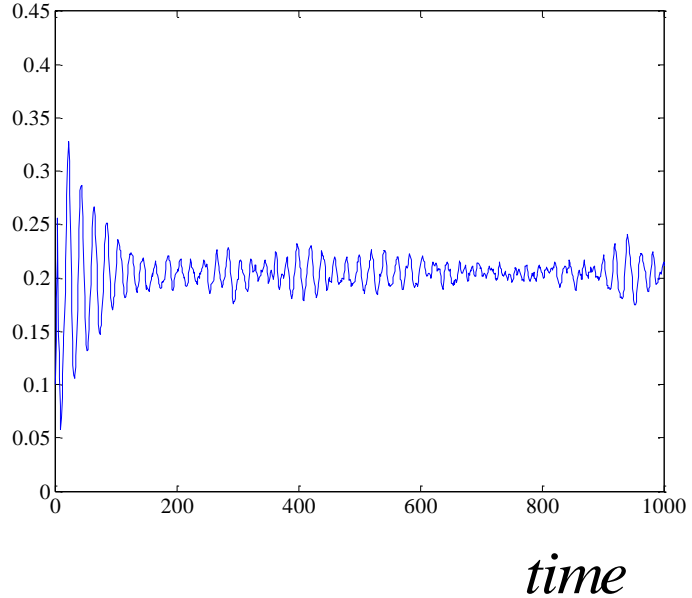
Nodes **B** and **C**: although they have the same number of connections, they have different clustering coefficients with node **C** being more likely to get infected earlier in the epidemic.

2. The importance of Network Topology

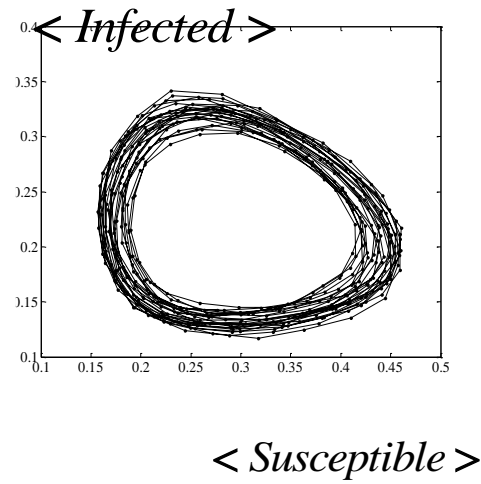
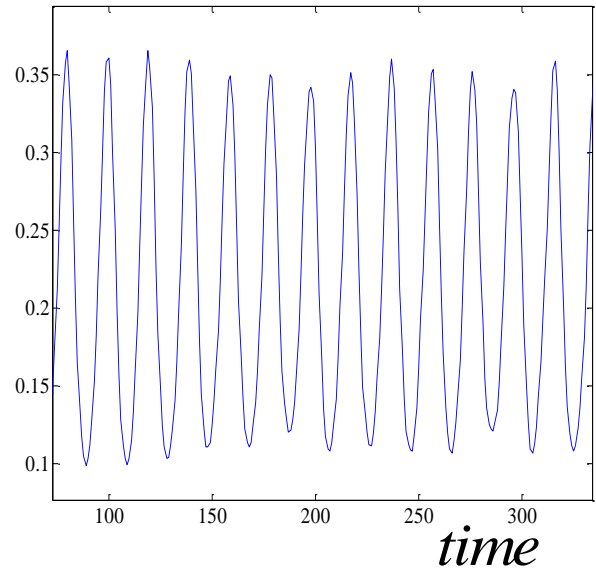


Contact transmission Network:
Watts and Strogatz Small World

Small-world network
constructed with $p=0.1$
density of susceptible



small-world network
constructed with $p=0.3$
density of susceptible



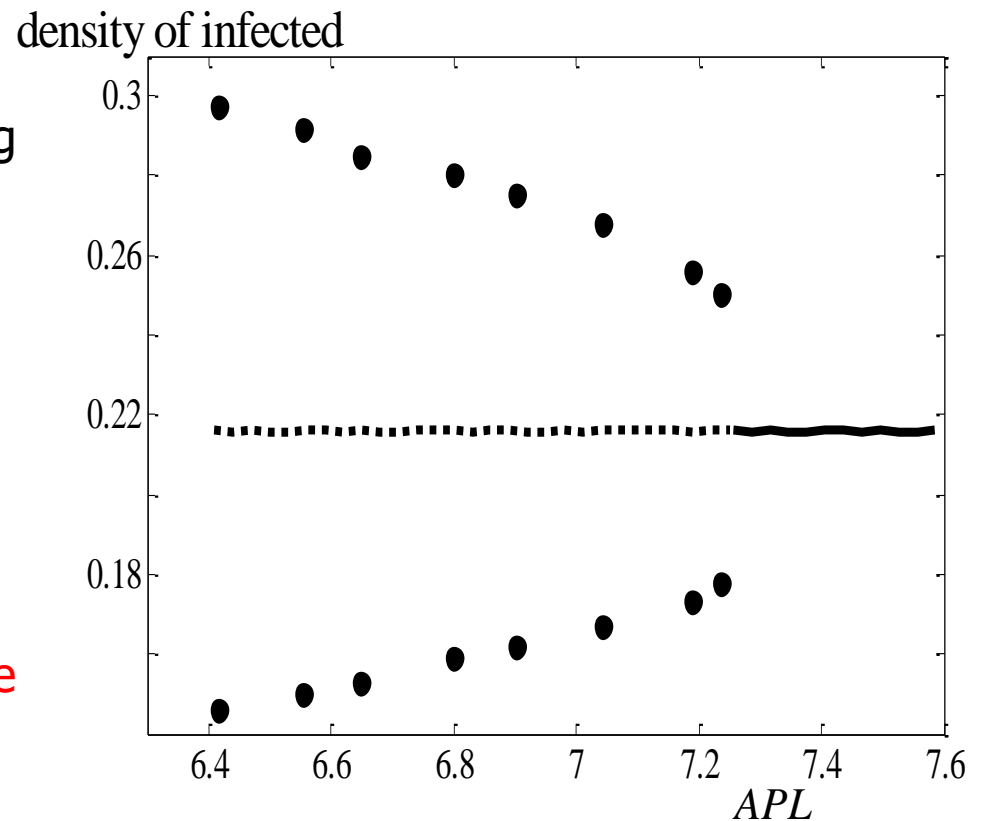
Coarse-grained Bifurcation diagram w.r.t the APL

Reppas, A.I., Spiliotis, K.G., Siettos, C.I., 2015, Tuning the Average Path Length of Complex Networks and its Influence to the Emergent Dynamics of the Majority-Rule Model, *Mathematics and Computers in Simulation*, 109, 186-196.

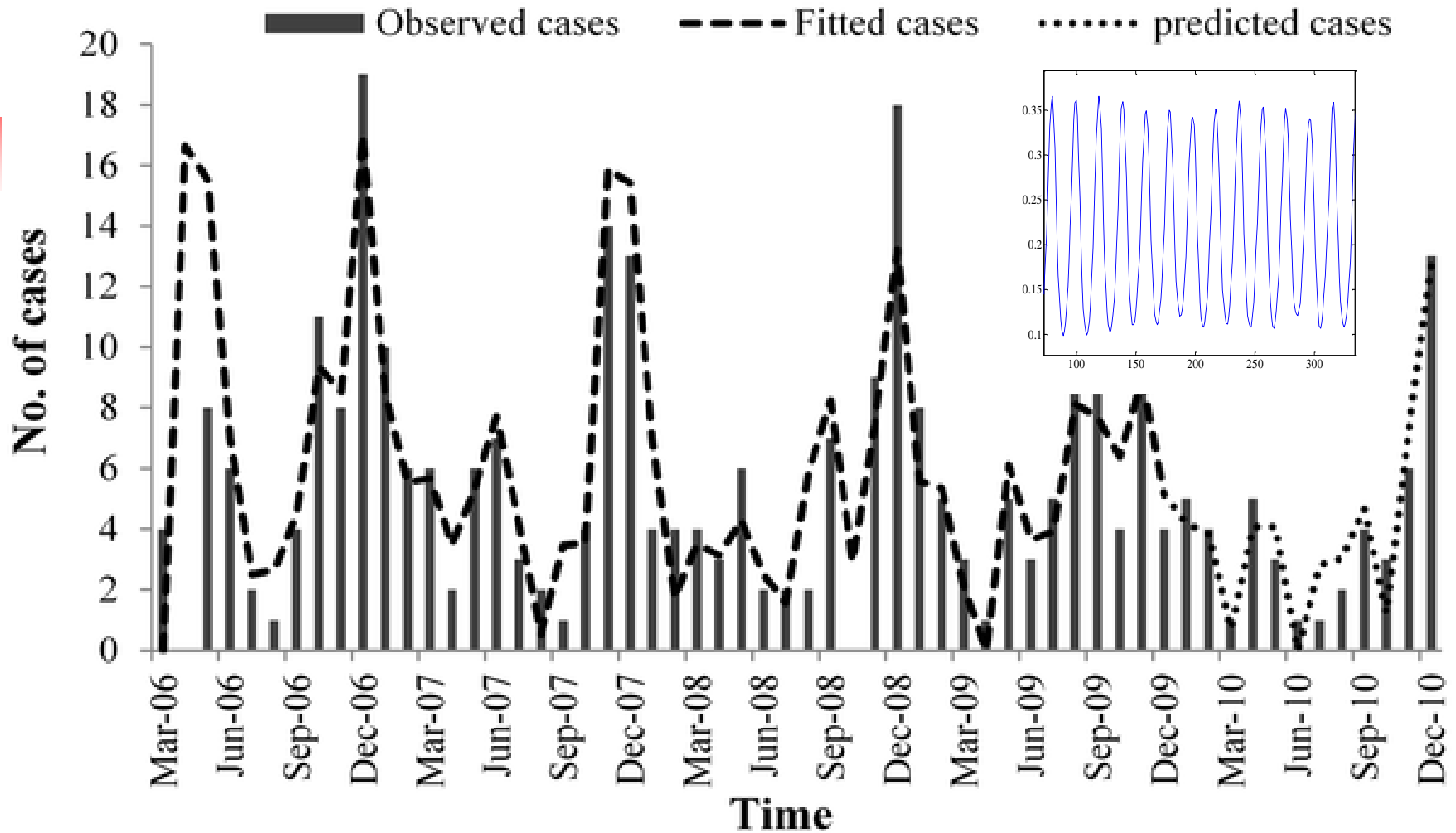
- We started with small-world networks constructed with a rewiring probability = 0.25

- Adjust the Average Path Length (APL); Degree and Clustering distributions are kept constant

- Equation-Free approach to trace the unstable branch



Hemorrhagic Fever with Renal Syndrome in Chenzhou, China



Xiao H, Tian H-Y, Gao L-D, Liu H-N, et al. (2014) Animal Reservoir, Natural and Socioeconomic Variations and the Transmission of Hemorrhagic Fever with Renal Syndrome in Chenzhou, China, 2006–2010. *PLoS Negl Trop Dis* 8(1): e2615. doi:10.1371/journal.pntd.0002615

<http://www.plosntd.org/article/info:doi/10.1371/journal.pntd.0002615>

3. Forecasting the EBOLA 2014-2015 Epidemics in West -Africa

The worst Ebola Virus Disease (EVD) epidemic in history ravaged West Africa.

- The epidemic began with the report of 49 cases and 29 deaths in Guinea on March 22, 2014.
- Liberia reported its first laboratory-confirmed cases on March 30, 2014,
- the first cases in Sierra Leone were reported on May 28, 2014.
- the virus crossed the local porous international borders, establishing chains of transmission not just in small villages, where it would have been easier to contain it, but also in large urban centers.
- Insufficient public health infrastructure, poor sanitation conditions, and unsafe traditional burial practices were the main reasons to the spread of the epidemic in the region.

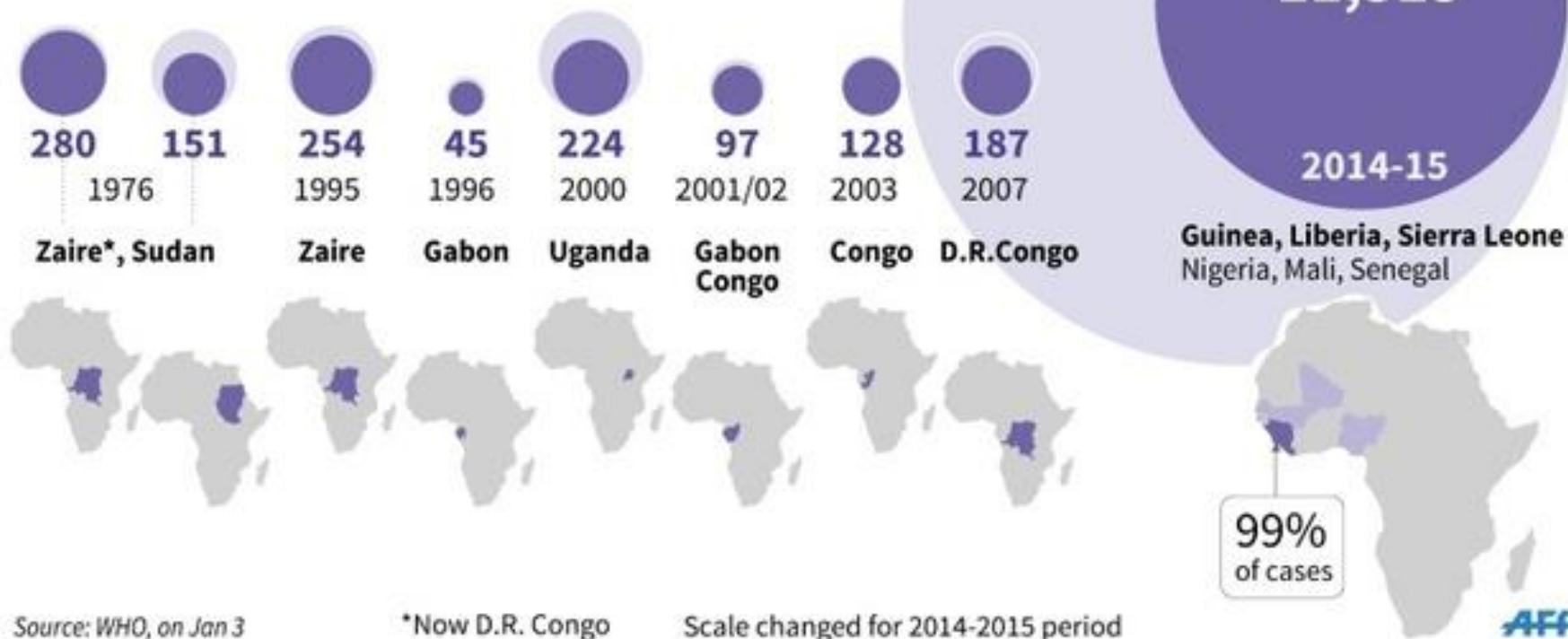
According to the WHO only the total death toll exceeded 17000 people.

The map of the Epidemic

The worst ebola outbreak in history

► Principal ebola outbreaks

● Cases ● Deaths



Mathematical Models: the Ebola Epidemic



- Both deterministic and stochastic SEIR dynamic models have been used to study the 1995 and 2000 Ebola outbreaks in DR Congo and Uganda, which were caused by the Zaire and Sudan virus strains, correspondingly (e.g. [Chowell et al., 2004](#); [Lecone and Finkenstädt, 2006](#)).
- [Legrand et al. \(2007\)](#), analyzed data from these two epidemics with a sixth-order stochastic compartmental model that incorporated explicitly the settings of transmission in the community, in the hospital and **during traditional burial ceremonies**.
- For the current Ebola outbreak in West Africa, [Rivers et al. \(2014\)](#) utilized the model proposed by Legrand (2007) to approximate and forecast the evolution of the spread in Liberia and Sierra Leone. **Their model forecasted a continuously increasing epidemic until December 31, 2014, with medians of 117,877 and 30,611 cases for Liberia and Sierra Leone, respectively.**

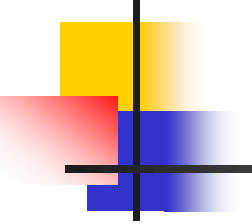


3. Forecasting the EBOLA 2014-2015 Epidemics in West -Africa

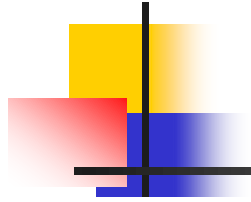
Factors such as:

- **Incubation period, recovery period, time to death,**
- **Per- Contact transmission probability (the most difficult to predict just from clinical studies)**
- **Reproductive number – number of secondary infected from an infectious!!!**
- **Age-Specific distributions (age-structured parameters)**
- **Topological characteristics of the underlying transmission network is of utmost importance,**

Mathematical Models: the Ebola Epidemic

- 
- **Althaus (2014)** used a deterministic SEIR dynamic model to estimate two vital epidemiological parameters for any infection, describing the spread of EBOV in West African countries, in this case: the basic and the effective reproduction numbers, R_0 and R_e
 - **A compartmental stochastic, individual-based model employed by Gomes et al. (2014)** to approximate the dynamics of the Ebola outbreak worldwide at an early period of the outbreak, estimated a rapid increase of the cases in African countries, and a potential international threat on a longer time-scale.
 - **Kiskowski (2014)** combined a stochastic SEIR model with a three-scale community network model representing contacts between households and local communities, to demonstrate that the different regional trends of the early growth dynamics of the 2014 EBOV epidemic in Guinea, Sierra Leone and Liberia might be explained by disparate local community mixing rates.

Mathematical Models: Our contribution



Computer model predicted when the Ebola outbreak in Liberia would fade out

Last updated: Monday 16 March 2015 at 2am PST

Ebola

Adapted media release

Infectious Diseases / Bacteria / Viruses

A novel mathematical approach applied to model the ongoing [Ebola](#) outbreak, predicted the current fade out of the epidemic in Liberia almost to the exact date (early March). Using World Health Organization (WHO) data through December 21, 2014, the study that was published online in *PLoS Currents Outbreaks*, was the first to provide an accurate prediction for the epidemic containment.



What's new

Siettos, C., Anastassopoulou, C., Russo, L., Grigoras, C., Mylonakis, E., 2015, [Modeling the 2014 Ebola Virus Epidemic – Agent-Based Simulations, Temporal Analysis and Future Predictions for Liberia and Sierra Leone](#). *PLOS Currents*, 2015 Mar 9.

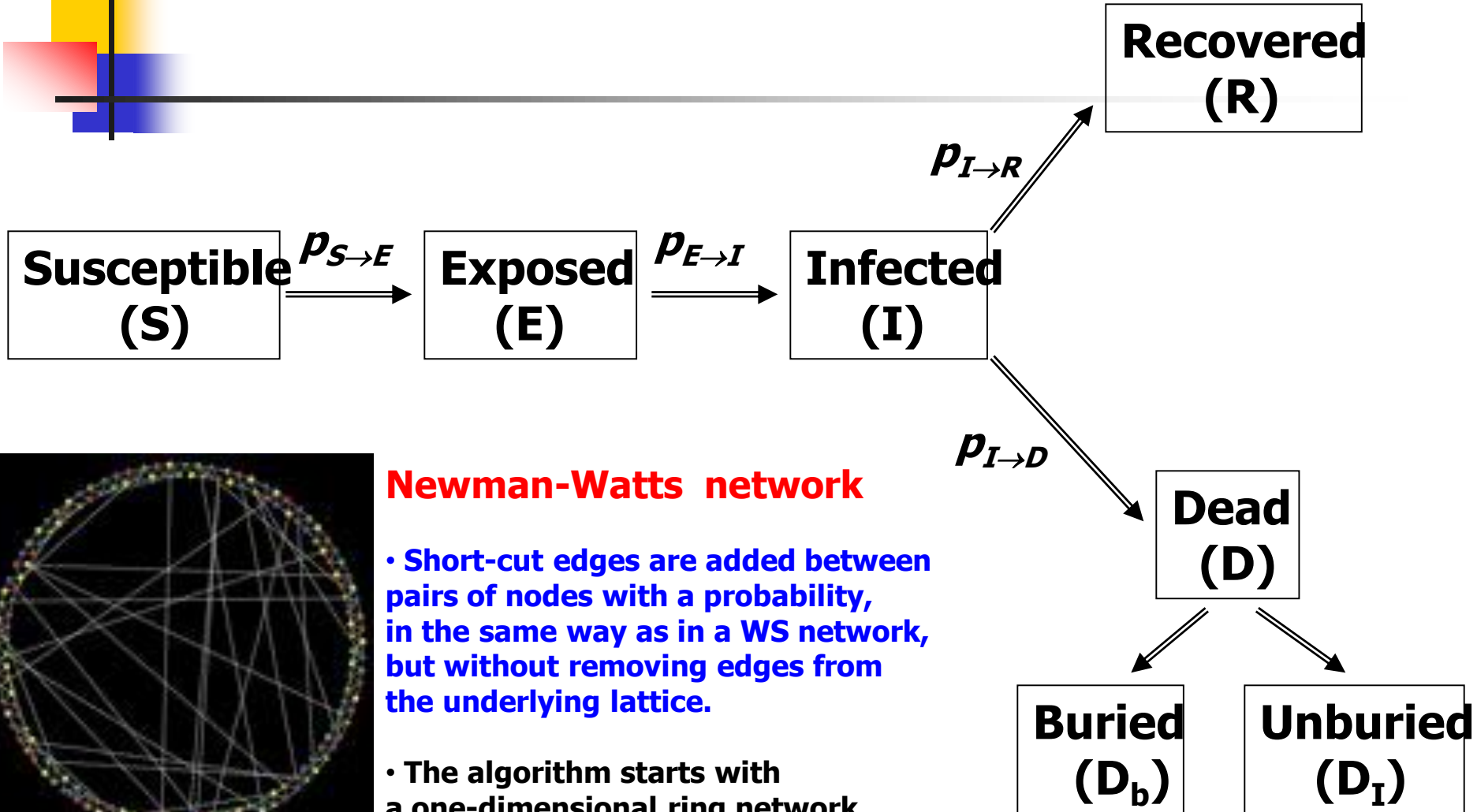
and also

Siettos, C., Anastassopoulou, C., Russo, L., Grigoras, C., Mylonakis, E., 2016, [Modeling, Forecasting and Control Policy Assessment for the Ebola Virus Disease \(EVD\) Epidemic in Sierra Leone Using Small-World Networked Model Simulations](#), *BMJ Open*, 6, e008649

Integrating **Agent-Based modeling** on complex networks and the so-called **Equation-Free** approach (multiscale bridging) which allowed us to assess various important epidemiologic parameters **including the evolution of the underlying transmission network**

Model and Methodology in a Nutshell

Number of Agents = Population $\sim O(4-6 \text{ millions})$



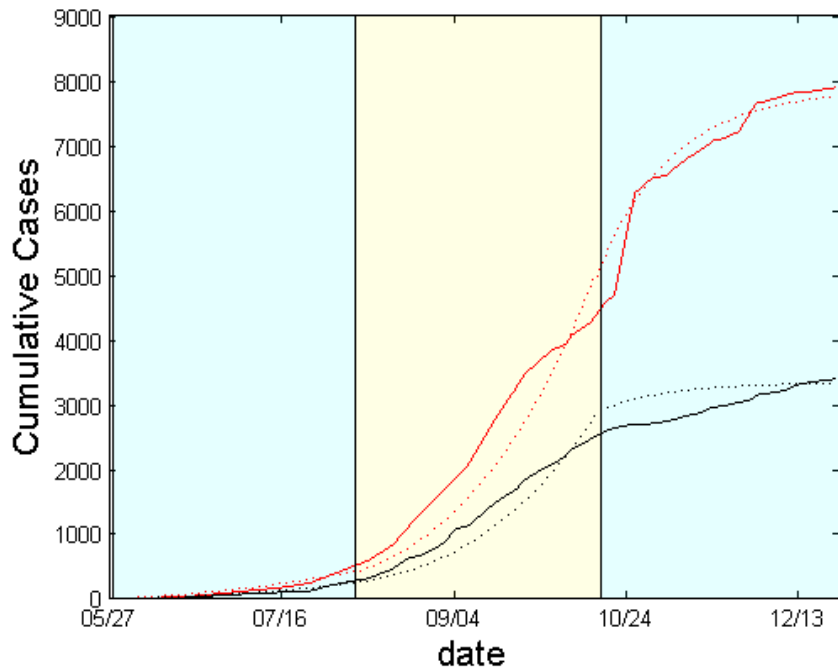
Forecasting the Evolution of EBOLA Epidemics: the case of Liberia and Sierra Leone



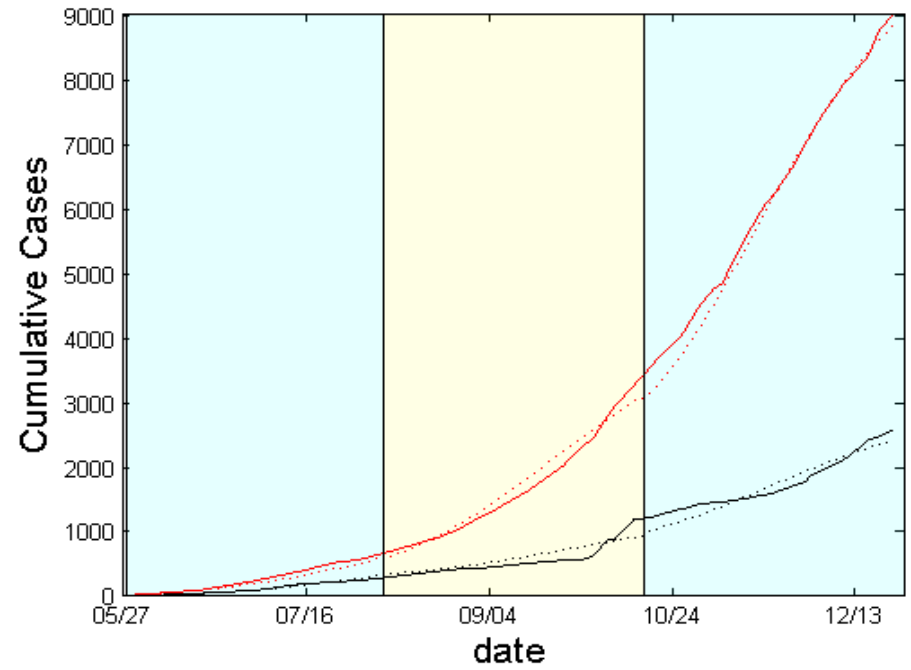
- **Time series of the official case counts from the World Health Organization were used for model fitting (CDC, 2014).**
- **Case data, which included cumulative incidence and cumulative deaths by date of report for Liberia and Sierra Leone retrieved on 5th of January, were found on Wikipedia (2015) and compiled from WHO case reports**
- **Simulations were performed using May 27, 2014 as an initial date and a time horizon of 70 days (10 weeks) with an equal sliding window time interval; the last date was December 21, 2014.**

RESULTS

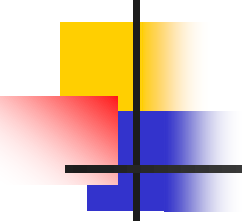
LIBERIA



SIERRA LEONE



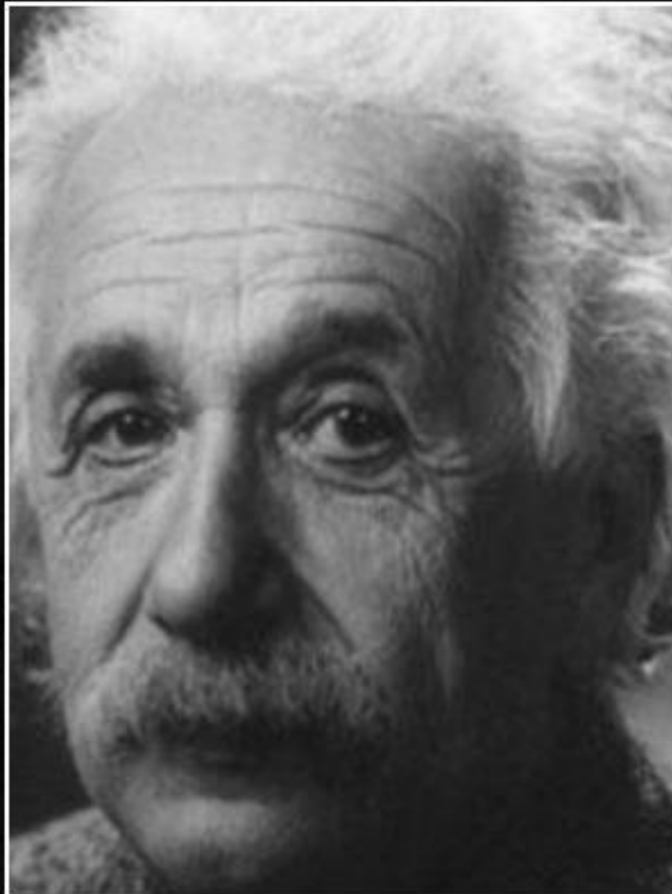
Conclusions



We propose an approach bridging state-of-the-art Agent-Based Models and Numerical Analysis/ Control Techniques for the risk assessment and forecasting of Emerging Infectious Dynamics

- We have successfully forecasted the evolution of the Epidemic in Liberia and Sierra Leone, ahead of time (a time horizon of 3 months)
- Usefulness of Would-Be Worlds/ Mathematical models should not be overestimated.
- Despite the significant technological progress and concentrated wealth, breakdowns and cuts in public health infrastructures worldwide are (the) major reasons for boosting epidemics.

Conclusions



We should be on our guard not to overestimate science and scientific methods when it is a question of human problems, and we should not assume that experts are the only ones who have the right to express themselves on questions affecting the organization of society.

— *Albert Einstein* —

AZ QUOTES

On one hand....



Number of doctors & nurses

per 100,000 population (WHO)



On the other hand....

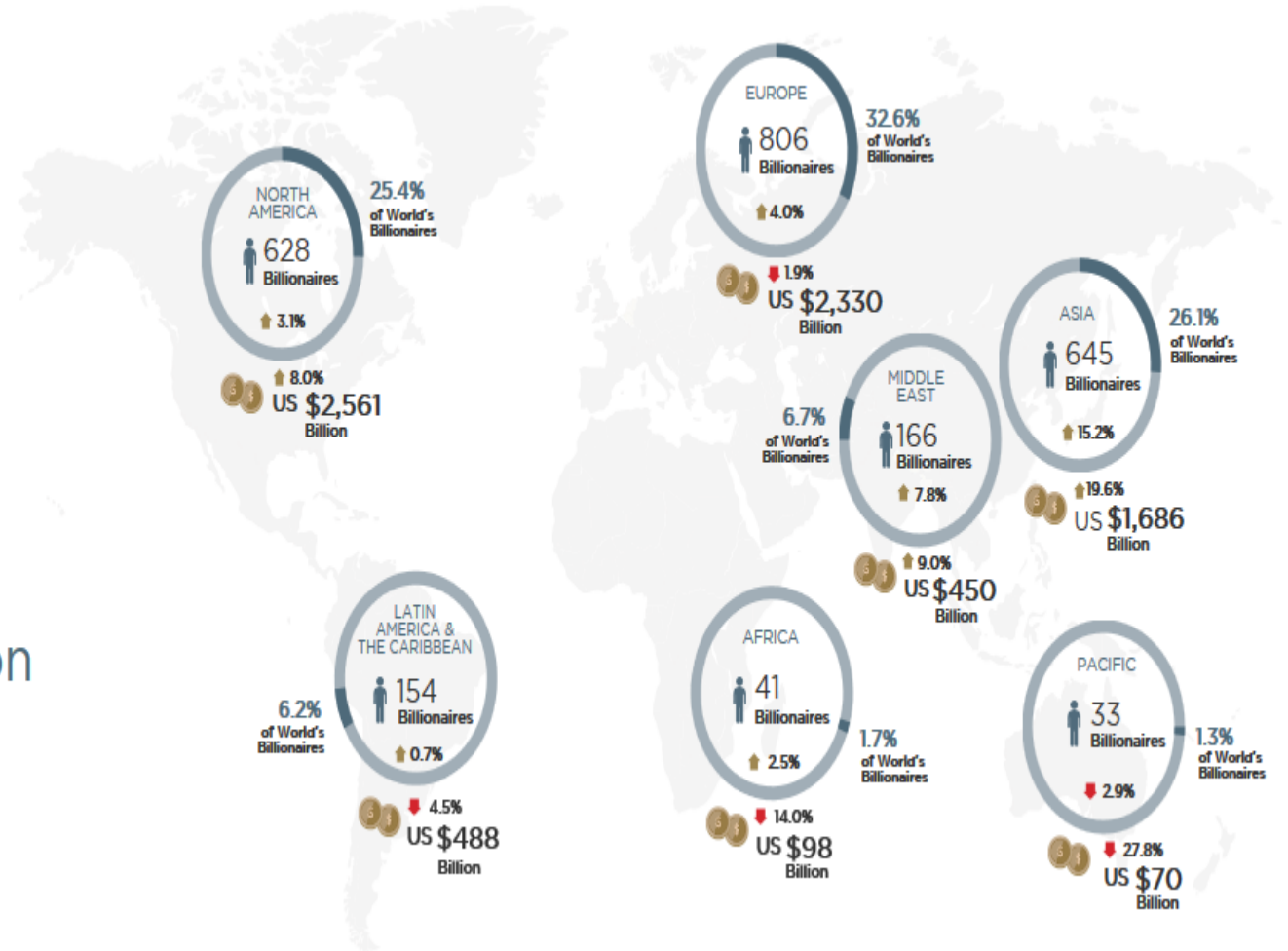


Wealth-X Billionaire Census 2015-16

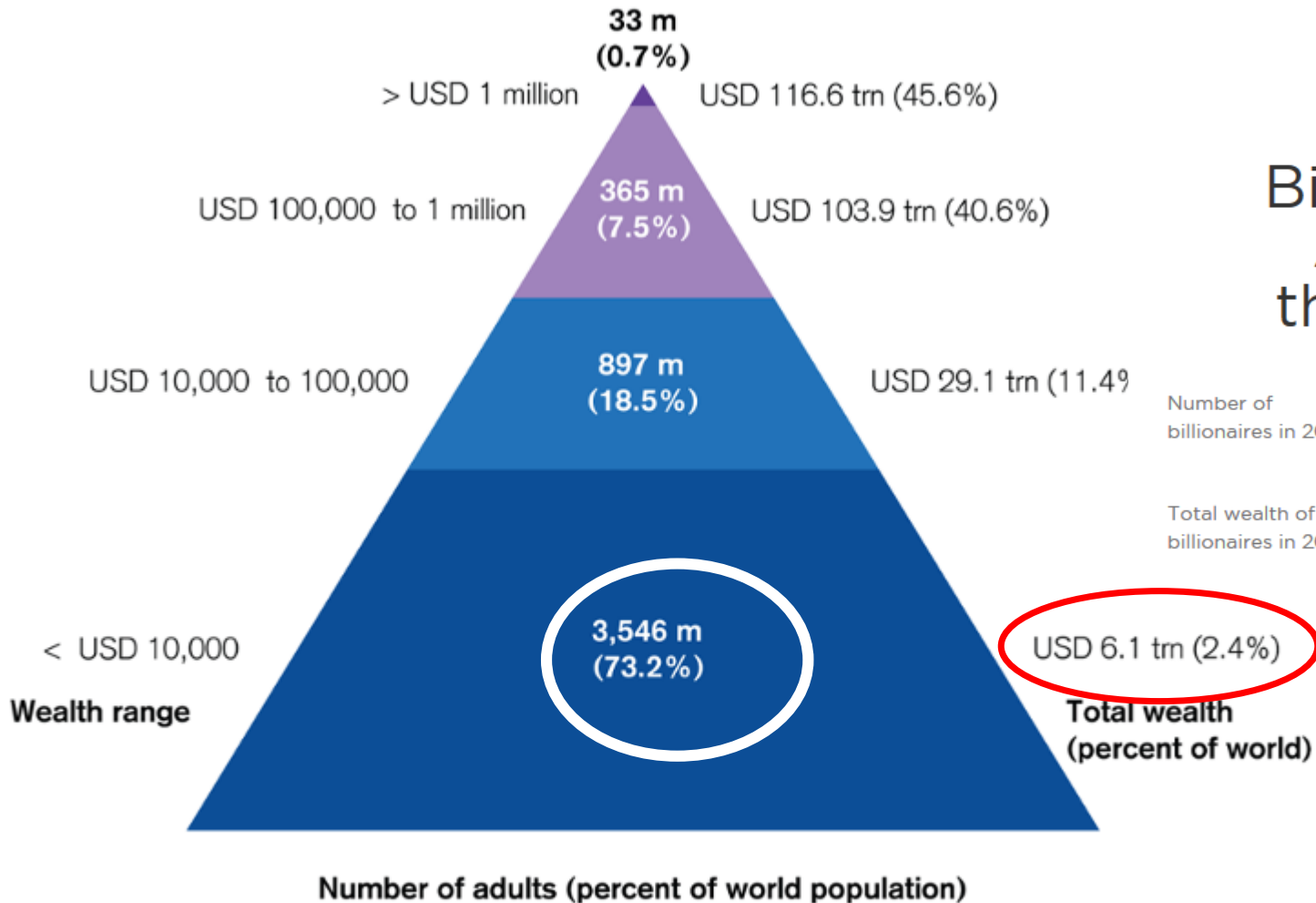
Billionaires Around the World

Number of
billionaires in 2015: **2,473**

Total wealth of
billionaires in 2015: **\$7.7 trillion**



The Global Wealth Pyramid



Billionaires Around the World

Number of billionaires in 2015:

2,473

Total wealth of billionaires in 2015:

\$7.7 trillion

USD 6.1 trn (2.4%)

Total wealth (percent of world)

The Global Wealth Pyramid

Source: James Davies, Rodrigo Lluberas and Anthony Shorrocks, Credit Suisse Global Wealth Databook 2016

Thank you!

